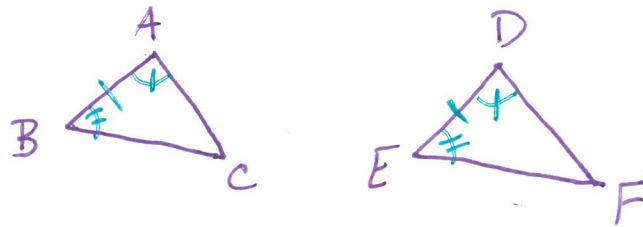


Thm 30



Given/Let $\triangle ABC$ and $\triangle DEF$ such that

$$\angle BAC \cong \angle EDF \text{ and}$$

$$\angle ABC \cong \angle DEF \text{ and}$$

$$\overline{AB} \cong \overline{DE}$$

$$\text{So } m\angle BAC = m\angle EDF \quad (1)$$

$$m\angle ABC = m\angle DEF \quad (2)$$

$$\underline{AB} = \underline{DE} \quad (3)$$

By Ax 3, there exists an isometry, f , such that (3.5)

$$f(A) = D \quad (4)$$

$$f(B) \in \overrightarrow{DE} \quad (5)$$

$f(C)$ is on the side of \overleftrightarrow{DE} that includes F . (6)

By Thm 26, $(\underline{3.5}, 4, \underline{5}, \underline{3})$ $f(B) = E$ (7)

By Thm 27 $(1, 3.5, 4, 5, 6)$ $f(C) \in \overrightarrow{DF}$ $\angle BAC$ (8)

By Thm 27 $(2, 3.5, \downarrow, 4, 6)$ $f(C) \in \overrightarrow{EF}$ $\angle ABC$ (9)

$$f(A) = D, \text{ so } f(A) \in \overrightarrow{ED}$$

$$F \in \overrightarrow{DF} \cap \overrightarrow{EF}$$

$$f(C) \in \overrightarrow{DF} \cap \overrightarrow{EF} \quad (10)$$

so by Thm 10 $f(C) = F$ (11)

By $(4, 7, 11)$ and Thm 18(a), $\triangle ABC \cong \triangle DEF$