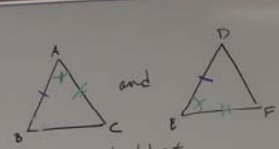


Let  be triangles

such that

$$(1) \overline{AB} \cong \overline{DE} \quad \overline{AC} \cong \overline{DF} \quad (1)$$

and $\angle BAC \cong \angle EDF$ (2)

By Th 3, there is an isometry f such that

$$f(A) = E \quad (3)$$

$$f(B) \in \overline{ED} \quad (4)$$

$$f(C) \text{ is on same side of } \overline{ED} \text{ as } F \quad (5)$$

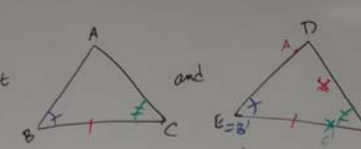
Let $f(A) = A'$, $f(B) = B'$, $f(C) = C'$

By (1) (by th 16) $d(A, B) = d(C, D)$
and by (2, 3) $f(B) = D$
thm 17a

By thm 18a, and... f has properties (3, 3, 4)
and $m(\angle BAC) = m(\angle DFE)$ (5)
so $f(C) \in \overline{EF}$ (6)

By thm 17a and (3), (4), (5), (6)
Thus $\triangle ABC \cong \triangle DEF$

By thm 17a and f has properties 2, 6
and $d(A, C) = d(E, F)$ by 7
So $f(C) = F$

Let  be triangles, such that

$$\angle ABC \cong \angle DEF \quad (1)$$

$$\overline{BC} \cong \overline{EF} \quad (2)$$

$$\angle ACB \cong \angle DFE \quad (3)$$

By Th 3 there is...
By Th 3 there is an isometry f such that

$$f(B) = E \quad (4)$$

$$f(C) \in \overline{EF} \quad (5)$$

$$f(A) \text{ on the same side of } \overline{EF} \text{ as } D \quad (6)$$

By Thm 17a (2, 4, 5)
so $f(C) = F$ $C' = F$ (7)

By thm 18a (1), (4, 5, 6)
 $A' \in \overline{ED}$ * (8)

By thm 15a and (7) $f(C) = F$
 $f(B) = B' \in \overline{FE}$
and (6) and (3)
* So $f(A) \in \overline{FD}$
 $f(A) \in \overline{DE}$
 $f(A) \in \overline{FD}$
so
 $f(A) \in \overline{DE} \cap \overline{FD}$
also $D \in \overline{DE} \cap \overline{FD}$
So by theorem 10 $f(A) = D$