## Geometry test 1 topics and problems:

1. Know how to use a compass and straight edge to transform a shape (eg. a triangle). Typical problem:

Rotate  $\triangle ABC$  around point *P* by angle  $\angle EDF$ , then reflect its image across line *PD* (note: there will be sufficient space on the test to do this).



2. Explain how to find a midpoint of a segment  $\overline{AB}$ 

3. Given a segment  $\overline{AB}$ , explain how to find a third point C so that  $\Delta ABC$  is equilateral

4. Explain how to move a triangle to a given place using compositions of rotations and translations Typical problem: Describe a set of rotations and/or translations that will map  $\Delta ABC$  so that the image of C is Dand the image of B is on ray  $\overrightarrow{DE}$  and the image of A is on the opposite side of  $\overrightarrow{DE}$  as F



5. Which of these outcomes can always be achieved by doing an isometry or a series of isometries? (For any set of non-collinear points A, B, C, D, E, F)?

D maps to $F$	A maps to $E$	A maps to $D$
$B$ maps to a point on $\overrightarrow{FA}$	$B$ maps to a point on $\overrightarrow{EF}$	$B$ maps to a point on $\overrightarrow{EF}$
C maps to a point on the same	C maps to a point on the same	C maps to a point on the same
side of $\overrightarrow{FA}$ as $D$	side of $\overrightarrow{DE}$ as $F$	side of $\overleftrightarrow{EF}$ as D

Which ones are impossible, and what is wrong with the instructions?

6. Use Axiom 3 to define a reflection across  $\overrightarrow{AB}$ 

7. Prove two sets are equal using distance properties:

typical problems:

a. Prove that the isometric image of a segment is a segment

b. Prove that the isometric image of a circle with radius 5 is a circle with radius 5.

c. Given that  $\Delta ABC$  is an equilateral triangle (all sides the same length), prove that the isometric image of A, B

and C are vertices of an equilateral triangle.