## Geometry test 1 topics and problems:

1. Know how to use a compass and straight edge to transform a shape (eg. a triangle).

Typical problem:
Rotate $\triangle A B C$ around point $P$ by angle $\angle E D F$, then reflect its image across line $\overleftrightarrow{P D}$ (note: there will be sufficient space on the test to do this).

${ }^{\bullet} \boldsymbol{P}$

2. Explain how to find a midpoint of a segment $\overline{A B}$
3. Given a segment $\overline{A B}$, explain how to find a third point $C$ so that $\triangle A B C$ is equilateral
4. Explain how to move a triangle to a given place using compositions of rotations and translations

Typical problem: Describe a set of rotations and/or translations that will map $\triangle A B C$ so that the image of $C$ is $D$ and the image of $B$ is on ray $\overrightarrow{D E}$ and the image of $A$ is on the opposite side of $\overleftrightarrow{D E}$ as $F$

5. Which of these outcomes can always be achieved by doing an isometry or a series of isometries? (For any set of non-collinear points $A, B, C, D, E, F)$ ?

| $D$ maps to $F$ | $A$ maps to $E$ | $A$ maps to $D$ |
| :--- | :--- | :--- |
| $B$ maps to a point on $\overrightarrow{F A}$ | $B$ maps to a point on $\overrightarrow{E F}$ | $B$ maps to a point on $\overrightarrow{E F}$ |
| $C$ maps to a point on the same | $C$ maps to a point on the same | $C$ maps to a point on the same |
| side of $\overleftrightarrow{F A}$ as $D$ | side of $\overleftrightarrow{D E}$ as $F$ | side of $\overleftrightarrow{E F}$ as D |

Which ones are impossible, and what is wrong with the instructions?
6. Use Axiom 3 to define a reflection across $\overleftrightarrow{A B}$
7. Prove two sets are equal using distance properties:
typical problems:
a. Prove that the isometric image of a segment is a segment
b. Prove that the isometric image of a circle with radius 5 is a circle with radius 5 .
c. Given that $\triangle A B C$ is an equilateral triangle (all sides the same length), prove that the isometric image of $A, B$ and $C$ are vertices of an equilateral triangle.

