Math 247 Final Exam topics:

There will be some questions on the new content, which includes:

- Finding areas that can be broken into rectangles and triangles on a grid.
- Finding perimeters on a grid
- Identifying the height given a triangle with an identified base
- Knowing some common errors:
- Error: counting dots instead of spaces for lengths
- Error: counting diagonal lengths the same as regular grid lengths
- Deciding that if a change to a shape makes the area smaller, then the area has to get smaller or vice versa (when the shapes are not similar)
- Relating lengths, areas, and volumes for similar shapes.
- Ratio problems (multiplicative comparison)

There will also be a lot of the test that is about fractions. In particular, you'll be answering questions about:

- Simplifying fractions
- Adding or subtracting fractions
- Multiplying fractions
- Dividing fractions

To understand and explain fractions and fraction operations, you can use some of the strategies we have practiced in this class:

- Writing word problems that work with both whole numbers and fractions
- Making fraction diagrams with units carefully labelled that match addition, subtraction, multiplication, partitive division or measurement division.
- Comparing the operations (multiplication, addition etc.) you do for the numerator and denominator in a diagram to the operations (multiplication, addition, etc.) you do for the numerator and denominator in a standard numerical algorithm
You are likely to be asked to do some or all of these steps for particular fraction operations.

Practice problems:

| 1. | original | scale factor | new |
| :--- | :--- | :--- | :--- |
| beak | 1 cm |  |  |
| wing | 4 cm |  | 12 cm |
| tail |  |  | 9 cm |
| Area |  |  | $99 \mathrm{~cm}^{2}$ |



| 2. | original | scale factor | new |
| :--- | :--- | :--- | :--- |
| trunk |  |  | 6 in |
| length | 24 in |  | 18 in |
| head | 4 in |  |  |
| area | 256 in $^{2}$ |  |  |


3. I have two similar/proportional pictures of a bus. If the smaller bus has area $15 \mathrm{~cm}^{2}$, and the area of the large bus is $60 \mathrm{~cm}^{2}$, what is the (length) scale factor that compares the large one to the small one?
4. Maya painted a tiger that was 12 inches high, and it used $1 / 2 \mathrm{oz}$ of paint. If she wants to enlarge her picture (proportionately) to make a mural 6 feet high, how much paint will she need? (this one is extra tricky)
5. Figure out the side lengths and find each of these perimeters. Show your work in a neat, easy to follow way (assume a 1 -cm grid size).

6. Find the areas of the shapes in \#5
7. Draw the heights that correspond to the bold base in these triangles:

8. For the word problems below:

- Draw a bar diagram (or similar bar diagram)
- Solve the problem by multiplying and dividing by whole numbers
- Write a fraction multiplication expression for the solution
a. In a bag of $\mathrm{M} \& \mathrm{Ms}$ there are $3 / 5$ as many red $\mathrm{M} \& \mathrm{Ms}$ as green $\mathrm{M} \& \mathrm{Ms}$. There are 15 red $\mathrm{M} \& \mathrm{Ms}$. How many green M\&Ms are there?
b. In a bag of M\&Ms there are $3 / 5$ as many red M\&Ms as green M\&Ms. There are 15 green M\&Ms. How many red M\&Ms are there?
c. Mike has $3 / 4$ of a quart of juice. Jane has $3 / 5$ as much juice as Mike. How much juice does Jane have?
d. Jane has $3 / 4$ of a quart of juice. Jane has $3 / 5$ as much juice as Mike. How much juice does Mike have?

9. Explain (using a diagram) how to simplify $12 / 15$
10. For the problem: $\frac{7}{8}-\frac{2}{3}$
a. Write a word problem
b. Show how to solve it with a diagram
c. Show how to solve it with a numerical algorithm
d. Explain how the diagram work matches the number work.
11. For the problem: $1 \frac{3}{8} \times \frac{3}{4}$
a. Write a word problem
b. Show how to solve it with a diagram
c. Show how to solve it with a numerical algorithm
d. Explain how the diagram work matches the number work.
12. For the problem: $1 \frac{3}{8} \div \frac{2}{3}$
a. Write a word problem
b. Show how to solve it with a diagram
c. Show how to solve it with a numerical algorithm
d. Explain how the diagram work matches the number work.
