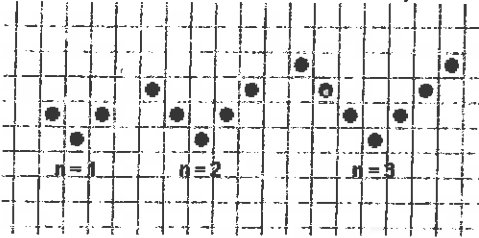


Some problems that use patterns.

Solve these on a separate sheet of paper.

1. In the dot pattern V-numbers, we discovered that there were $d=2n+1$ dots in the n th pattern.



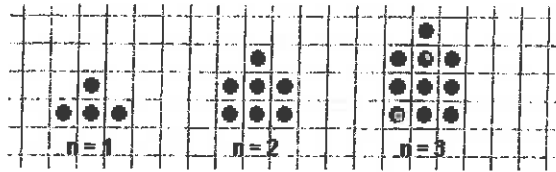
There is 1 dot at the bottom of the pattern, and 2 sets of n dots, one on either side.

- At what step (n) of the pattern are there 101 dots?
- What is the highest pattern step (n) that you could make with 84 dots?
- What is the highest pattern step (n) that you can make with A dots? (make sure you explain what to do if you have a remainder when dividing)
- What is the smallest pattern step (n) that would include at least 140 dots?
- What is the smallest pattern step (n) that would include at least B dots? (explain remainders)
- If you solved e using an equation, show how to solve by reasoning about the pattern. If you solved e by reasoning, show how to solve using the equation.

2. At the convention, each attendee gets a badge. There are 3 badge holders left over from the previous convention, and then new packages of badge holders are opened. Badge holders come in packages of 8.

- Find an equation telling how many badge holders there are available if n packages are opened. Explain the equation.
- If there are 20 people at the convention, how many packages of badge holders will be opened?
- If there are 100 people at the convention, how many packages of badge holders will be opened?
- If there are N people at the convention, how many packages of badge holders will be opened?
- If you solved d using an equation, show how to solve by reasoning about the pattern. If you solved d by reasoning, show how to solve using the equation.

3. For the dot pattern tower numbers:



- Find and explain an equation for tower numbers (how many dots in pattern n)
- Is there a tower that has exactly 100 dots? If so, how many stories does it have? If not, how do you know?
- How many stories tall (n) would the shortest tower be that had at least 264 dots?
- How many stories tall (n) would the shortest tower be that had at least A dots?
- How many stories tall (n) would the highest tower you could make with 126 dots be?
- How many stories tall would the highest tower you could make with B dots be?
- If you solved f using an equation, show how to solve by reasoning about the pattern. If you solved f by reasoning, show how to solve using the equation.

4. In a pattern block train made with trapezoids, the perimeter of a train made with n blocks is $p=3n+2$, because each of the n trapezoids have 3 units on the top and bottom, and there are 2 more units on the left and right ends of the train.

- Is there a trapezoid train that has a perimeter of exactly 100 units? If so, how many blocks does it take to make the train? If not, how do you know it's impossible?
- How many pattern blocks would it take to make a train that has a perimeter of at least 234 units?
- How many pattern blocks would it take to make a train that has a perimeter of at least P units?
- If you are only allowed a maximum perimeter of 150 units, how many pattern blocks would it take to make the longest such train?
- If you are only allowed a maximum perimeter of P units, how many pattern blocks would it take to make the longest such train?
- If you solved e using an equation, show how to solve by reasoning about the pattern. If you solved e by reasoning, show how to solve using the equation.

840
1255
→ round down
round up

#1

$$d = 2n + 1$$

a. 101 dots?

$$\begin{aligned} \underline{n=50} \quad 2n+1 &= 101 \\ -1 \quad -1 \\ 2n &= 100 \\ n &= \frac{100}{2} = \mathbf{50} \end{aligned}$$

b. Highest possible with only 84 dots?

$$\begin{aligned} 2n+1 &= 84 \\ -1 \quad -1 \\ 2n &= 83 \\ n &= 83/2 = 41.5 \\ &\quad \text{41 RI} \end{aligned}$$

41 → 83 dots 42 → 85 dots?
 round down: 41 dots = n

d. at least 140 dots

$$\begin{aligned} 2n+1 &= 140 \\ -1 \quad -1 \\ 2n &= 139 \\ n &= 69 \text{ RI round up: } 70 = n \end{aligned}$$

c. use A instead of 84

10 am

$$\begin{aligned} 2n+1 &= A \\ -1 \quad -1 \\ 2n &= A-1 \\ \frac{2n}{2} &= \frac{A-1}{2} \end{aligned}$$

$$n = \frac{A-1}{2} \quad n = (A-1) \div 2$$

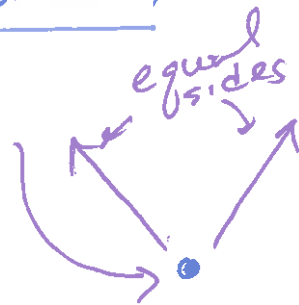
If n has a remainder then don't use the remainder (round down)

$$\begin{aligned} e. \quad 2n+1 &= B \\ -1 \quad -1 \\ 2n &= B-1 \\ \frac{2n}{2} &= \frac{B-1}{2} \end{aligned}$$

$$n = (B-1) \div 2$$

If n has a remainder then round up (add 1 to the quotient) to get at least B (B or more)

$\underbrace{B-1}_{\text{dots left}} \leftarrow$ use 1 dot for middle



$(B-1) \div 2 \rightarrow$ equal amount for both sides

Round up to the next whole number so we can use all B dots.

10 am

2a) n packages open

↓ badges

$$b = 8n + 3$$

↑
badges

↑

↑
Number of packages

← Num badges I have already

per package

b) 20 people → 3 packages

give 3 badges (17 people left)

open 1st pkg. give 8 badges (9 people)

open 2nd pkg. give 8 (1 person)

open 3rd pkg. give 1 done

$$8n + 3 = 20$$

$$\begin{array}{r} -3 \\ -3 \end{array}$$

$$8n = 17$$

$$n = \frac{17}{8} = 2 \text{ R } 1$$

round

up to 3

$$c). \quad 8n + 3 = 100$$

$$\begin{array}{r} -3 \\ -3 \end{array}$$

$$8n = 97$$

$$n = \frac{97}{8} = 12 \text{ R } 1 \rightarrow 13 \text{ packages.}$$

$$d) \quad 8n + 3 = N$$

$$\begin{array}{r} -3 \\ -3 \end{array}$$

$$\frac{8n}{8} = \frac{N-3}{8}$$

$$n = \frac{N-3}{8}$$

→ If there is a remainder then

Round up to next whole number.

2e) If I have N people

10 am

I give 3 badge holders to first 3 people.

$N-3$ people left.

$$\underbrace{(N-3) \div 8}$$

how many 8's are in $N-3$

Make groups of 8, so open $(N-3) \div 8$
~~badge~~ boxes.

If there's any remainder, open 1 more box (round up)