

1 day old caterpillar

2 day old caterpillar

3 day old caterpillar

Build a 4 and 5 day old caterpillar

1 day old caterpillar

2 day old caterpillar

3 day old caterpillar

Fill in a table showing how many blocks you need to build each caterpillar

days old			total
1	4	1	5
2	8	1	9
3	12	1	13
4	16	1	17

grade K strategy is build and count

grade 1 strategy is count and then add (count on)

grows +4 stays the same every time

days old			total
1			5
2			
3			
4			
5			
10	4x10	+1	41
100	4x100	+1	401

grade 3 strategy is find a pattern and multiply

grade 2 strategy is find a pattern and add on

add 4 9 times

More third grade questions:

- How many pattern blocks are in 1 car? *easier*
- How many pattern blocks would you need to make 5 cars?
- If you made a train and you used 8 green triangles, how many blue rhombi would you need?
- If you made a train and you used 14 blue rhombi, how many green triangles would it have?
- Could you make a train that used 5 blue rhombi? *harder*
(Explain your answer)

Common Core Math Practice Standards

- [MP1](#) Make sense of problems and persevere in solving them.
- [MP2](#) Reason abstractly and quantitatively.
- [MP3](#) Construct viable arguments and critique the reasoning of others.
- [MP4](#) Model with mathematics.
- [MP5](#) Use appropriate tools strategically.
- [MP6](#) Attend to precision.
- [MP7](#) Look for and make use of structure.
- [MP8](#) Look for and express regularity in repeated reasoning.

Common Core Math Practice Standards

MP8 Look for and express regularity in repeated reasoning.

$2+3=3+2$
commutative law

days old			total
1	4		5
2	4+4		9
3	3x4		13
4	4x4		17
5	5x4		21
10			
100			

Handwritten notes: $+4$, $+4$, $+4$, $+4$, $+4$, $+4$

Common Core Math Practice Standards

MP7 Look for and make use of structure.



3. If you made a train and you used 8 green triangles, how many blue rhombi would you need?

Handwritten answer: 2 rhombi for each triangle
↓
double the number of triangles

Common Core Math Practice Standards

MP6 Attend to precision.

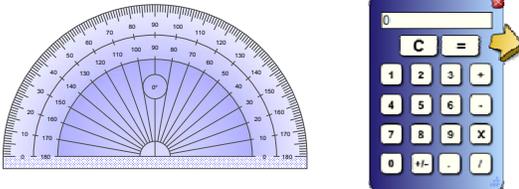
Handwritten note: be careful with academic language

Handwritten note: Label tables and graphs

days old			total
1			
2			
3			
4			
5			
10			
100			

Common Core Math Practice Standards

MP5 Use appropriate tools strategically.



Common Core Math Practice Standards

MP4 Model with mathematics.



number of chirps in 14 seconds + 40°F

Handwritten note: using number equations to describe things

days old			total
1			
2			
3			
4			
5			
10			
100			

Handwritten note: $4 \times 100 + 1 = 401$

Handwritten note: "In early grades, this might be as simple as writing an addition equation to describe a situation."

Common Core Math Practice Standards

MP3 Construct viable arguments and critique the reasoning of others.

Handwritten note: share & learn from each other's strategies

days old			total
1			5
2			
3			
4			
5			
10	40	1	41
100			

Handwritten notes: 10 sets of 4 triangles = 40 triangles. Add 1 for the square makes 41. start with 5 and add 4 9 times

Common Core Math Practice Standards

MP2 Reason abstractly and quantitatively.

Decontextualize

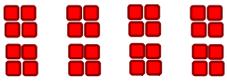
I can find how many crayons by multiplying 4×8



Context/descriptions
→ numbers

Contextualize

I know that 32 tells me how many crayons in all. I can interpret 4×8 as 4 sets of 8



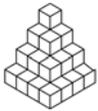
numbers
context

MPI **Make sense of problems and persevere in solving them**

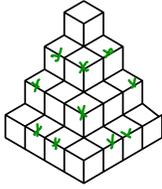
When presented with a problem, I can make a plan, carry out my plan, and evaluate its success.

BEFORE...	DURING...	AFTER...
EXPLAIN the problem to myself. <i>Have I solved a problem like this before?</i>	PERSEVERE	CHECK <i>Is my answer correct? How do my representations connect to my algorithm?</i>
ORGANIZE information... <i>What is the question I need to answer? What is given? What is not given? What are the relationships between known and unknown quantities? What tools will I use? What prior knowledge do I have to help me?</i>	MONITOR my work CHANGE my plan if it isn't working out ASK myself, "Does this make sense?"	EVALUATE <i>What worked? What didn't work? How was my solution similar to or different from my classmates'?</i>

- There are 4 separate large boxes, and inside each large box there are 3 separate small boxes, and inside each of these small boxes, there are 2 separate smaller boxes. How many boxes, counting all sizes, are there altogether?
- When asked how many gold coins he had, the collector said: **Math Olympiad problems (grades 4-8)**
If I arrange them in stacks of five, none are left over
If I arrange them in stacks of six, none are left over
If I arrange them in stacks of seven, one is left over
What is the least number of coins he could have?
- Alice and Betty run a 50-meter race, and Alice wins by 10 meters. They then run a 60-meter race, and each girl runs at the same speed she ran in the first race. By how many meters will Alice win?
- The tower at the right has no gaps. Suppose it is painted red on all exterior sides, including the bottom, and then cut into cubes along the indicated lines. How many cubes will each have red paint on just 3 faces?



- The tower at the right has no gaps. Suppose it is painted red on all exterior sides, including the bottom, and then cut into cubes along the indicated lines. How many cubes will each have red paint on just 3 faces?



and 1 in back!

With just cups, you can practice numbers and fine motor skills at the same time!



<http://lookatmyhappyrainbow.com/cups/>

cubes ■ ■ ■ ■	cups ■	With cups and cubes you can ask addition and subtraction questions: I had 6 cubes I hid some under the cup How many are under the cup?
5 in the cup 2 outside the cup		

How many cubes in all?



cubes

How much to show?

Show 2 repetitions to make it clear what the pattern is

cubes

Naming repeating patterns

AB

ABC

ABBA

A B C D

cubes

cups

Questions to ask

What is under the next cup?
 What is under cup number 8?
 What is under cup number 11?
 What is under cup number 20?

Kindergarteners can solve problems by touching cups and counting out patterns
 Second and third graders can use a number line to make deductions (eg. odd numbers are blue)

cubes

cups

What numbers go with the red tiles? *multiples of 3*
 What numbers go with the blue tiles? *1, 4, 7, ... skip count by 3*

What number comes next?

3, 6, 9, 12, 15, ___

4, 7, 10, 13, 16, ___

11, 21, 31, 41, 51, ___

4, 10, 16, 22, 28, ___

Typical related skip-count problems (gr. 3)

ABB B
ABCD

all patterns are 4 units long.

g p Y
 g p p
 g p p p
 g p p p p
 g p p p p p
 p p p p p p

Tile Design 1: Hmong Design in Border Mat B

Basic Pattern Is it complete (Y or N)

g p Y
 g p p
 g p p p
 g p p p p
 p p p p p

Prediction: Create a new basic pattern that you predict will be complete:

Test it out. Did your prediction work? Explain:

In order to make a completed pattern border, what must be true about the basic tile pattern?