

\mathbb{R}^3 : $\{(1, 1, 0), (0, 0, 1), \dots\}$ independent, but do they span \mathbb{R}^3 ?

$$\begin{bmatrix} 1 & 0 & | & x \\ 1 & 0 & | & y \\ 0 & 1 & | & z \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & | & x \\ 0 & 1 & | & z \\ 0 & 0 & | & x-y \end{bmatrix} \rightarrow \text{not always } 0?$$

Try $\langle 3, 2, 1 \rangle$

$$\begin{bmatrix} 1 & 0 & | & 3 \\ 1 & 0 & | & 2 \\ 0 & 1 & | & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & | & 3 \\ 0 & 1 & | & 1 \\ 0 & 0 & | & 1 \end{bmatrix} \quad \begin{array}{l} x=3 \\ y=1 \\ 0=1 \text{ yikes!} \end{array}$$

spanning set:

$$\{a(1, 1, 0) + b(0, 0, 1) \mid a, b \in \mathbb{R}\}$$

$$= \{(a, a, b) \mid a, b \in \mathbb{R}\}$$

$\{(1, 2, 0)\}$ spans a line: $(x, 2y, 0)$ 1 vector: most I get is a line

$\{(1, 1, 1), (1, 1, 0)\}$ spans a plane 2 vectors: most I get is a plane

$\{(1, 1, 1), (1, 1, 0), (1, 0, 0)\}$ spans \mathbb{R}^3 3 vectors: most I get is a 3 dimensional space

* To span, I need at least as many vectors as dimensions.

* Important ① How to use a matrix to tell if linearly independent.
② need at least as many vectors as dimensions to span
(write up) ③ Use a matrix to check for spanning