Some circle practice problems
From EngageNY:
Find the value of $x$ in each figure below, and describe how you arrived at the answer.

## 1. Hint: Thales' theorem


2.

4.


## 5. From Khan Academy:

In the figure below, $\angle A B C$ is inscribed in circle $P$. The length of $\overline{P C}$ is 12 units. The arc length of $\overparen{A C}$ is $\frac{68}{15} \pi$.


What is the measure of $\angle A B C$ in degrees?
6. Also from EngageNY:

Opening Exercise
In a circle, a chord $\overline{D E}$ and a diameter $\overline{A B}$ are extended outside of the circle to meet at point $C$. If $m \angle D A E=46^{\circ}$, and $m \angle D C A=32^{\circ}$, find $m \angle D E A$.

7.

8.


## Problem 1

Find the value of $x$ in the following diagram:


## Problem 2

Find the value of $x$ in the following diagram:


## Problem 3

In a circle, chords $A B$ and $C D$ intersect at $R$. If $A R: B R=1: 4$ and $C R: D R=4: 9$, find the ratio $A B: C D$.


## Problem 4

Chords $A B$ and $C D$ of a given circle are perpendicular to each other and intersect at a right angle at point $E$. Given that $B E=16, D E=4$, and $A D=5$, find $C E$.

## Problem 1

Two tangents from an external point $P$ are drawn to a circle and intersect it at $A$ and $B$. A third tangent meets the circle at $T$, and the tangents $\overrightarrow{P A}$ and $\overrightarrow{P B}$ at points $Q$ and $R$, respectively (this means that T is on the minor arc $A B$ ). Find the perimeter of $\triangle P Q R$.

## Problem 2

Square $A B C D$ of side length 10 has a circle inscribed in it. Let $M$ be the midpoint of $\overline{A B}$. Find the length of that portion of the segment $\overline{M C}$ that lies outside of the circle.

