

Understanding Theorem 1.4

First do an example:

- a. Find integers greater than 1 such that $a \mid bc$ and $(a,b) = 1$. Is it true that $a \mid c$?

$a =$

$b =$

$c =$

And a non-example:

- b. Find integers greater than 1 such that $a \mid bc$ and $(a,b) = 2$ where $a \nmid c$?

$a =$

$b =$

$c =$

Now understand the proof:

Let, a, b, c be integers such that $a \mid bc$ and $(a,b) = 1$

Why do we know that there exists an integer r such that $bc = ar$?

Why do we know that there exist integers u and v such that $au + bv = 1$?

Which of these equations lets us say that $c = acu + bcv$? What did we do to it?

How do we get to the equation: $c = a(cu + rv)$?

Does $c = a(cu + rv)$ mean that $a \mid c$ or that $c \mid a$?