

1. Fill out the operation table for the permutation group S_3

$f \circ g$ do first (g) \rightarrow do second (f) \downarrow	$\begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix}$	$\begin{pmatrix} 1 & 2 & 3 \\ 1 & 3 & 2 \end{pmatrix}$	$\begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix}$	$\begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \end{pmatrix}$	$\begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$
$\begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix}$						
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$\begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{pmatrix}$						
$\begin{pmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \end{pmatrix}$						
$\begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$						

a. Is S_3 abelian? Give an example of this from your table.

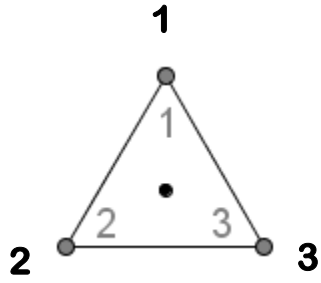
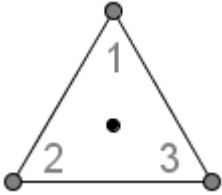
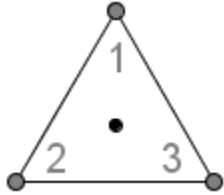
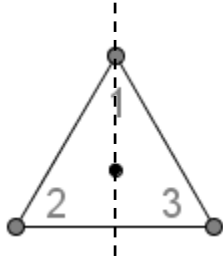
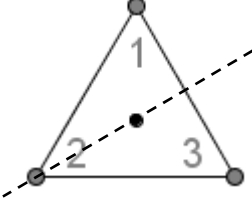
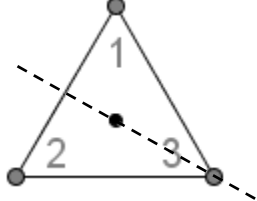
b. What is the identity element for S_3 ?

c. List the inverses of each of these elements:

i. $\begin{pmatrix} 1 & 2 & 3 \\ 1 & 3 & 2 \end{pmatrix}^{-1} = \begin{pmatrix} 1 & 2 & 3 \\ & & \end{pmatrix}$ ii. $\begin{pmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \end{pmatrix}^{-1} = \begin{pmatrix} 1 & 2 & 3 \\ & & \end{pmatrix}$

iii. $\begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix}^{-1} = \begin{pmatrix} 1 & 2 & 3 \\ & & \end{pmatrix}$ iv. $\begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix}^{-1} = \begin{pmatrix} 1 & 2 & 3 \\ & & \end{pmatrix}$

2. Write in where each vertex ends after the transformation shown

<p>$e = \text{identity map}$ rotate 0°</p> 	<p>$r_1 = \text{rotate } 120^\circ$ counterclockwise</p> 	<p>$r_2 = \text{rotate } 240^\circ$ counterclockwise</p> 
<p>$v = \text{reflect in the vertical line}$</p> 	<p>$u = \text{reflect in the line shown}$</p> 	<p>$w = \text{reflect in the line shown}$</p> 

Fill out the operation table for the dihedral group D_3 of rigid transformations of the equilateral triangle

$f \circ g$ do first (g) \rightarrow do second (f) \downarrow	e	r_1	r_2	v	u	w
e						
r_1						
r_2						
v						
u						
w						

Is D_3 abelian? How do you know?

What is the inverse of each element?

$$e^{-1} = \quad v^{-1} =$$

$$r_1^{-1} = \quad u^{-1} =$$

$$r_2^{-1} = \quad w^{-1} =$$

Each of the elements can be written as a composition of r_1 and v . For example $r_2 = r_1 \circ r_1$. Find a way to get u and w using r_1 and v .

$u =$

$w =$