

17. $S =$ ordered pairs of real numbers

$$z = (3, -4) \in S$$

$$(x_1, x_2) R (y_1, y_2) \text{ if } x_1^2 + x_2^2 = y_1^2 + y_2^2$$

$$(x, y) R (a, b) \text{ if } x^2 + y^2 = a^2 + b^2$$

Equiv Relation?

Reflexive? $(x, y) R (x, y)$ because $x^2 + y^2 = x^2 + y^2$

Symmetric? If $(x, y) R (a, b)$, then $x^2 + y^2 = a^2 + b^2$
so $(a, b) R (x, y)$ because $a^2 + b^2 = x^2 + y^2$

Transitive? If $(x, y) R (a, b)$ and $(a, b) R (p, q)$

$$\text{So } x^2 + y^2 = a^2 + b^2 \quad \text{and} \quad a^2 + b^2 = p^2 + q^2$$

$$\text{so } x^2 + y^2 = p^2 + q^2$$

$$\text{So } (x, y) R (p, q)$$

$$[(3, -4)] = \{(x, y) \mid x^2 + y^2 = 25\}$$

\downarrow circle w/ radius 5
center at $(0, 0)$

Infinite number of equiv-classes.