

Math 166 review for test 3:

1. Do everything (max, min, increasing, decreasing, inflection points, concavity, and horizontal asymptotes for:

$y = \sin^2 x + 2\sin x$  in the interval  $[0, 3\pi]$

2. Find these infinite limits:

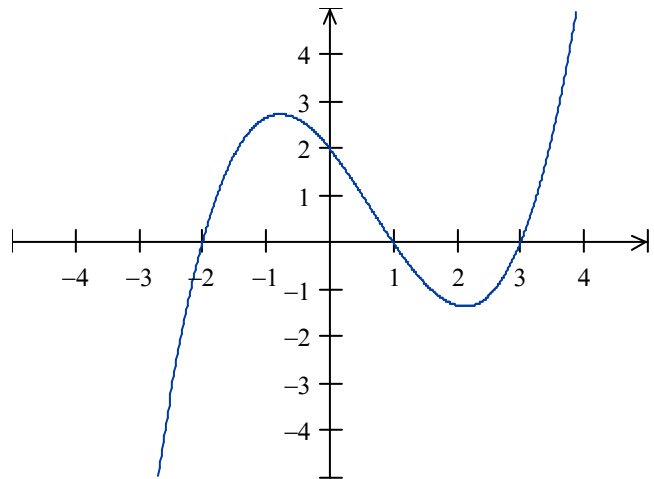
$$\lim_{x \rightarrow -\infty} \frac{2x+5}{\sqrt{4+9x^2}} \qquad \lim_{x \rightarrow \infty} \sqrt{4x^2+5x} - 2x$$

3. Find the absolute max and mins for:

a. Find the absolute maxima and minima for:  $y = x + 2\sin(x)$   $[-\pi, 2\pi]$

b. Find the absolute maxima and minima for:  $y = x^{7/5} - 3x^{2/5}$   $[-1, 2]$

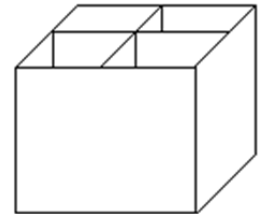
4. Tell the x-coordinates of the local maxima and local minima of  $f(x)$ , given this graph of  $f'(x)$



*There will be at least one max/min problem in an applied context; probably a box problem, and fairly probably a weight or a cost problem.*

5. I want to make a box with a square base and an open top that has the greatest possible volume, with a surface area of  $9\text{ft}^2$ . What should the dimensions of my box be?

6. I want to make a box with a square base and an open top that is subdivided into 4 sections inside as shown. I need the volume of my box to be  $2\text{ft}^3$ . What should the dimensions of my box be so that I use the least material in constructing it? (assume that the subdivisions are made of the same material as the sides and base of the box)



7. I want to make a box with a square base and an open top that is subdivided into 4 sections inside as shown in #6. I need the volume of my box to be  $2\text{ft}^3$ . The sides and base of the box weigh  $6\text{oz}/\text{ft}^2$ , and the material I use to construct the inner subdivisions weighs  $3\text{oz}/\text{ft}^2$ . What should the dimensions of my box be so that it weighs the least?

8. I want to make a box with a base whose length is 1.5 times its width, and with a lid whose volume is  $3\text{ft}^2$ . The material for the base and sides costs  $\$.40$  per  $\text{ft}^2$ , and the cardboard for the lid costs  $\$.70$  per  $\text{ft}^2$ . What dimensions give me the cheapest box?

b. I want to make a box with a square base and an open top that is subdivided into 4 sections inside as shown in #12. I need the volume of my box to be  $2\text{ft}^3$ . The cardboard for the sides and base of the box costs  $\$.50$  per  $\text{ft}^2$ , and the cardboard for the insert sections costs  $\$.20$  per  $\text{ft}^2$ . What dimensions give me the cheapest box?