Math 146 Chapter 1 test practice

Solve each equation:

1.
$$\frac{1}{3}x + 5 = \frac{1}{4}(x+2)$$
 2. $2(3x-1) - (x+4) = x-3$ 3. $0.2x + 3.1 = 0.4(3x+8.2)$

(round to 2 decimal places)

4. Solve for t:
$$V = a^2rt + \frac{bt}{2} + n$$
 5. Solve for k: $D = (n-k)rt$
6. Solve by factoring: $2x^2 - 5x - 12 = 0$

7. Solve and leave the answer in exact simplified form (square roots, fractions, but no decimals) a. $2x^2 - 2x + 3 = 0$ b. $x^2 + 4x - 8 = 0$

Factor each expression:

8. a. $x^2 + 4x$ b. $x^3 - 10x^2 + 24x$ c. $6x^2 + 11x + 4$

Solve each equation:

9.
$$\frac{x+1}{x^2-9} - \frac{x+3}{x^2+5x+6} = \frac{4}{x^2-x-6}$$
 10. $(x+3)^{2/3} = 36$

Solve each inequality. Tell the answer using interval notation.

11.
$$2x + 5 \le 4x + 13$$
 12. $x^2 + 4x > 21$

Solve the absolute equations and inequalities. Give inequality answers in interval notation.

13.
$$|2x+5| = 4$$
 14. $\left|\frac{x+3}{2}\right| \le 4$ 15. $|4(x-7)| \ge 2$

Solve the following application problems:

16. a. A cube of ironwood has a volume of 22.8 mL, and a weight of 15.0 g. What is its density in g/mL? Round your answer to 3 significant figures

b. A carved figure made of ironwood has weight 8.5 g. Find the volume of the figure.

17. An ideal gas satisfies the equation PV=nRT, where P is the pressure in atm, V is the volume in Liters, T is the temperature in degrees kelvin, n is the number of moles, and R is a constant.

a. Solve for the constant R.

b. Air inside a 30 L. scuba canister is compressed to a pressure of 200 atmospheres. If the gas is released container with volume 150 L., what will the pressure of the gas be? (assume temperature does not change). c. CaCO3 decomposes at ~12200 K to form CO2 gas and CaO. If 25.0 L of CO2 are collected at 12200 K , what will the volume of this gas be after it cools to 500K?

18. A sample containing 0.63 M CO2 and 0.57 M H2 is allowed to equilibrate at 700 K. The final amount x of H₂O and CO is given by $\frac{x^2}{(0.57-x)(.63-x)} = 0.11$. Solve for x.

Answers:

1. -54
2. 3/4
3. -0.18
4.:
$$\frac{2V-2n}{2a^2r+b} = t$$

5. $k = n - \frac{D}{rt}$
6. $2x^2 - 5x - 12 = 0$ $(2x+3)(x-4) = 0 \implies x = 4, -3/2$
7. a. $x = \frac{1 \pm i\sqrt{5}}{2}$ alternate form: $x = \frac{1}{2} \pm \frac{i\sqrt{5}}{2}$ b. $x = -2 \pm 2\sqrt{3}$
8. a. $x^2 + 4x = x(x+4)$ b. $x^3 - 10x^2 + 24x = x(x-6)(x-4)$ c. $6x^2 + 11x + 4 = (3x+4)(2x+1)$

9. -1

10. 213 and -219 (for technical reasons, 213 without the alternate solution -219 would also be accepted as the correct answer)

11. $[-4,\infty)$ 12. $(-\infty,-7) \cup (3,\infty)$ 13.-1/2, -9/2 14. [-11,5] 15. $(-\infty,13/2] \cup [15/2,\infty)$

16. a. 0.658 g/mL b. 12.9 mL

17. b.
$$R = \frac{PV}{nT}$$
 b. $\frac{(200 \text{ atm})(30L)}{nT} = \frac{P(150L)}{nT} \implies P = 40 \text{ atm}$
c. $\frac{P(25L)}{n12200K} = \frac{PV}{n500K} \implies V = 1.02L$

 $\frac{x^2}{(0.57 - x)(.63 - x)} = 0.11 \implies x^2 = .11(0.57 - x)(.63 - x) \implies x^2 = .11x^2 - 0.132x + .039501$ $\implies 0.89x^2 + 0.132x - 0.039501 = 0 \implies x = \frac{-.132 \pm \sqrt{.132^2 - 4(.89)(-0.039501)}}{2 \cdot .89}$ $x \approx .15$