Math 146 Review for Half-Exam on Chapter 3:

1. List all of the possible rational zeros of a polynomial, such as $f(x)=3 x^{4}-2 x^{3}+7 x+10$
2. Completely factor a polynomial, given some information about some of the roots:
a. $f(x)=2 x^{4}-x^{3}-3 x^{2}$
b. $f(x)=x^{3}-x^{2}-11 x+3$ given -3 is a zero.
c. $f(x)=6 x^{3}+11 x^{2}-57 x-20$ given -4 is a zero
3. Graph each of these functions. Include your work showing how you figured out:

- Zeros
- Vertical asymptotes (if any)
- A sign chart
- End behavior
a. $y=x(x+2)^{2}(2 x-3)$
b. $y=(x-1)^{2}(x-3)^{3}(x+2)$
c. $y=\frac{(x+1)^{2}}{(x-1)(x+4)}$
d. $y=\frac{(2 x+1)(x-4)}{(x-1)(x-3)}$
e. $y=\frac{x}{(x-3)(x+2)}$

4. Write an equation of a function that will have the graph behavior shown (it should agree on zeros and signs):
a.

b.

